

1. A pin of length 1 is dropped onto the coordinate plane. Given that the pin falls flat at an angle α with the positive x -axis, what is the probability that the pin touches at least one of the lines $y = n$, where n is any integer? Justify your answer.
2. A pin of length 1 is dropped onto the coordinate plane. What is the probability that the pin touches at least one of the lines $y = n$, where n is any integer? Justify your answer. *Note:* As opposed to the previous problem, the pin can make any angle with the positive x -axis in this problem.
3. (*extra*) Redo Problems 1 and 2 above to find the probability that the pin touches at least one of the horizontal lines $y = n$ and at least one of the vertical lines $x = m$, where m and n are any integers.
4. (*extra*) Use the results Problems 1, 2 and 3 above to find the probability that the pin touches at least one of the horizontal lines $y = n$ or at least one of the vertical lines $x = m$, where m and n are any integers.